

SIGMABUDGIE · GRADE 4

Number Reasoning

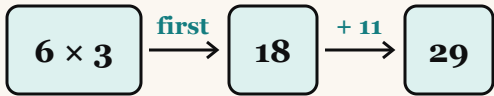
A gentle walkthrough & a 24-question exam

Part 1 walks through order of operations, factors, riddles, and working backwards from the very beginning, with drawings. Part 2 is a 24-question exam that starts easy and slowly builds to harder, ISEE-style reasoning questions. Work through the lesson together first, then let your child try the exam. The answer key at the back explains every question.

1 · Multiply before you add

$11 + 6 \times 3$ is not 17×3 . Multiplication and division go **first**, then addition and subtraction. $6 \times 3 = 18$, then $11 + 18 = \mathbf{29}$.

$20 - 8 \div 2$: $8 \div 2 = 4$ first, then $20 - 4 = \mathbf{16}$. Brackets beat everything: $(20 - 8) \div 2 = 6$.



$$11 + 6 \times 3 = 29$$

2 · Factors

A **factor** divides a number with nothing left over. Factors of 36: 1, 2, 3, 4, 6, 9, 12, 18, 36. Find them in pairs: 1×36 , 2×18 , 3×12 , 4×9 , 6×6 .

"Which is a factor of 48?" Test each choice: does $48 \div$ it come out even?

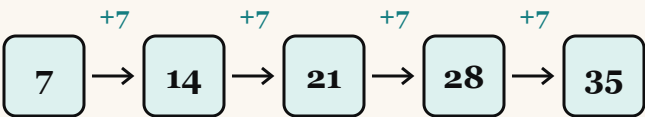
pairs	for 36
1×36	2×18
3×12	4×9
6×6	

factor pairs of 36

3 · Multiples

A **multiple** is what you get by multiplying: multiples of 7 are 7, 14, 21, 28, 35... Multiples of 5 end in 0 or 5. Multiples of 10 end in 0.

A number that is a multiple of both 4 and 6: 12, 24, 36. The smallest is **12**.



multiples of 7

4 • Odd and even rules

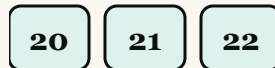
Even + even = even. Odd + odd = even. Even + odd = **odd**. Any number $\times$ even = even. Odd $\times$ odd = odd.

So the sum of two odd numbers is always even, and $3 \times 7 \times 9$ must be odd. You can rule out choices without calculating.

5 • Consecutive numbers

Consecutive means in a row: 20, 21, 22. "Three consecutive numbers add up to 63." The middle number is $63 \div 3 = 21$, so they are 20, 21, 22. The largest is **22**.

For three in a row, the middle one is always the total $\div 3$.

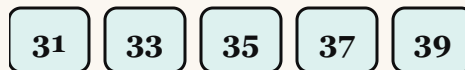


$$20 + 21 + 22 = 63$$

6 • Number riddles

"A number is greater than 29, less than 40, is odd, and its digits add up to 10." Take the clues in order. Between 29 and 40: 30 to 39. Odd: 31, 33, 35, 37, 39. Digits add to 10: $3 + 7 = 10$. The number is **37**.

Each clue crosses out more numbers. Keep a list.



odd numbers in the 30s; only 37 has digits that add to 10

7 • Working backwards, two steps

"A number is multiplied by 6, then 4 is subtracted, giving 50." Undo in reverse order: add 4 back (54), then divide by 6 (**9**).

If the question then asks for **double** the number, do not stop at 9: $2 \times 9 = \mathbf{18}$. Read the last sentence twice.



forwards

backwards: the number is 9

8 • Two-rule machines

"Put in 5 → 15, put in 9 → 23." Try $\times 2 + 5$: $5 \times 2 + 5 = 15$ ✓, $9 \times 2 + 5 = 23$ ✓. So 14 gives $14 \times 2 + 5 = \mathbf{33}$.

Trick to find the rule: when the In goes up by 1, how much does the Out go up? That number is the multiplier.

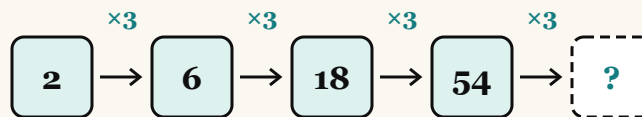
In	Out
5	15
9	23
14	?

rule: $\times 2 + 5$, so $14 \rightarrow 33$

9 • Patterns that multiply

2, 6, 18, 54: each number is $\times 3$ the one before. Next: **162**.

If the gaps grow fast, suspect multiplying. If the gaps are the same, it is adding.



next: 162

10 • Halfway and between

"Exactly halfway between 200 and 800": add and halve, $(200 + 800) \div 2 = \mathbf{500}$. Or half the gap: $600 \div 2 = 300$, then $200 + 300$.

It works for any two numbers: halfway between 720 and 1,320 is 1,020.

11 • Which must be true?

"Sam has more than Ali. Ali has more than Kim." What **must** be true? Sam has more than Kim. What **might** be true but is not forced? Kim has 5.

Pick only what the clues force. If you can imagine a case where it fails, it is not "must."



most to least

12 • Estimate, then check

Before choosing an answer, ask "about how big should it be?" 23×14 is about $20 \times 15 = 300$, so 322 is believable and 3,220 is not.

A quick estimate catches most slips. You are ready for the test! 🎉

Read each drawing first, then choose the best answer. Take your time, there is no clock here. Questions start gentle and get harder toward the end. Circle your answer.

1 What is $11 + 6 \times 3$?

A 51

B 20

C 29

D 39

2 Which of these is a factor of 36?

A 9

B 5

C 7

D 8

3 Which is a multiple of 7?

A 27

B 17

C 32

D 28

4 What comes next? 2, 6, 18, 54, ____



A 108

B 162

C 58

D 72

5 What is $20 - 8 \div 2$?

A 16

B 6

C 12

D 4

6 Which number is exactly halfway between 200 and 800?

A 400

B 600

C 500

D 300

7 Three consecutive numbers add up to 63. What is the largest?

A 21

B 22

C 23

D 20

8 A machine's rule: put in 5 $\rightarrow$ 15, put in 9 $\rightarrow$ 23. What does 14 give?

In	Out
5	15
9	23
14	?

A 28

B 42

C 38

D 33

9 What is $11 + 3 \times 5$?

A 70

B 19

C 26

D 56

10 Which of these is a factor of 48?

A 6

B 5

C 7

D 9

11 A number is greater than 29, less than 40, is odd, and its digits add up to 10. What is it?

31	33	35	37	39
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A 35

B 39

C 33

D 37

12 Which sum is always even?

A odd + even

B odd + odd

C even + odd

D odd + 1

13 What is the smallest number that is a multiple of both 4 and 6?

A 12

B 24

C 10

D 48

14 Which number is exactly halfway between 720 and 1,320?

A 1,000

B 1,070

C 1,020

D 920

15 A number is multiplied by 6, then 4 is subtracted, giving 50. What is double the number?



A 9

B 18

C 27

D 108

16 A machine's rule: put in 4 → 22, put in 7 → 34. What does 13 give?

A 52

B 64

C 46

D 58

17 What is $(11 + 6) \times 3$?

A 29

B 39

C 20

D 51

18 Sam has more marbles than Ali. Ali has more than Kim. Which statement MUST be true?

A Kim has more than Sam.

B Sam has more than Kim.

C Ali has the most.

D Kim has exactly 5.

19 Four consecutive numbers add up to 50. What is the smallest?

A 11

B 12

C 10

D 13

20 How many factors does 16 have?

A 4

B 3

C 5

D 8

21 A number is doubled, then 7 is added, giving 31. What is the number?

A 19

B 12

C 24

D 15

22 A machine's rule: put in 6 $\rightarrow$ 16, put in 7 $\rightarrow$ 18. What does 13 give?

A 26

B 36

C 32

D 30

23 Which of these is odd?

A $3 \times 7 \times 8$

B $2 + 3 + 5$

C $3 \times 7 \times 9$

D 4×11

24 A two-digit number is a multiple of 9 and a multiple of 4, and it is less than 50. What is it?

A 36

B 45

C 18

D 72

ANSWER KEY & EXPLANATIONS

- 1 C** Multiply first: $6 \times 3 = 18$. Then $11 + 18 = 29$.
-
- 2 A** $36 \div 9 = 4$ exactly. The others leave remainders.
-
- 3 D** $7 \times 4 = 28$.
-
- 4 B** Each number is $\times 3$: $54 \times 3 = 162$.
-
- 5 A** Divide first: $8 \div 2 = 4$. Then $20 - 4 = 16$.
-
- 6 C** $(200 + 800) \div 2 = 500$.
-
- 7 B** The middle is $63 \div 3 = 21$, so the numbers are 20, 21, 22.
-
- 8 D** The rule is $\times 2 + 5$. $14 \times 2 + 5 = 33$.
-
- 9 C** $3 \times 5 = 15$, then $11 + 15 = 26$.
-
- 10 A** $48 \div 6 = 8$.
-
- 11 D** Odd numbers in the 30s: 31, 33, 35, 37, 39. Only $3 + 7 = 10$.
-
- 12 B** Two odd numbers always add to an even number, like $3 + 5 = 8$.
-
- 13 A** Multiples of 4: 4, 8, 12. Multiples of 6: 6, 12. The first shared one is 12.
-
- 14 C** The gap is 600, half is 300. $720 + 300 = 1,020$.
-
- 15 B** Undo: $50 + 4 = 54$, $54 \div 6 = 9$. Double 9 is 18.
-
- 16 D** In goes up 3, Out goes up 12, so $\times 4$. $4 \times 4 = 16$, plus 6 = 22. Rule: $\times 4 + 6$. $13 \times 4 + 6 = 58$.
-
- 17 D** Brackets first: $11 + 6 = 17$. Then $17 \times 3 = 51$.
-
- 18 B** Most to least: Sam, Ali, Kim. So Sam has more than Kim.
-
- 19 A** $11 + 12 + 13 + 14 = 50$.
-
- 20 C** 1, 2, 4, 8, 16: five factors. (4×4 counts only once.)
-
- 21 B** Undo: $31 - 7 = 24$, $24 \div 2 = 12$.
-
- 22 D** In up 1, Out up 2: $\times 2$. $6 \times 2 = 12$, plus 4 = 16. Rule $\times 2 + 4$. $13 \times 2 + 4 = 30$.
-
- 23 C** Odd $\times$ odd $\times$ odd is odd (189). The others have an even factor or an even sum.
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- 24 A** Multiples of 9 under 50: 9, 18, 27, 36, 45. Only 36 is also a multiple of 4.
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