

SIGMABUDGIE · GRADE 4

Area, Perimeter & Angles

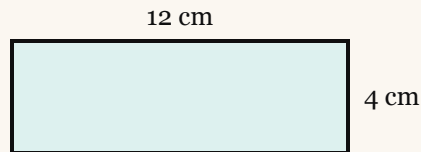
A gentle walkthrough & a 24-question exam

Part 1 walks through area, perimeter, angles, and shapes from the very beginning, with drawings. Part 2 is a 24-question exam that starts easy and slowly builds to harder, ISEE-style reasoning questions. Work through the lesson together first, then let your child try the exam. The answer key at the back explains every question.

1 · The two formulas

Perimeter is the distance around: add all four sides, or $2 \times (\text{length} + \text{width})$. **Area** is the space inside: $\text{length} \times \text{width}$.

A 12 cm by 4 cm rectangle: perimeter $2 \times (12 + 4) = \mathbf{32 \text{ cm}}$. Area $12 \times 4 = \mathbf{48 \text{ square cm}}$.

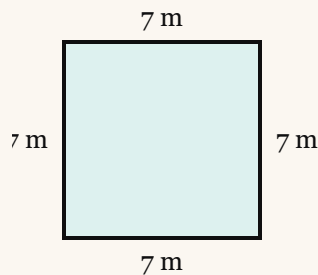


$$P = 32 \text{ cm}, A = 48 \text{ sq cm}$$

2 · Squares: one number tells all

A square has 4 equal sides. Side 7: perimeter $4 \times 7 = \mathbf{28}$, area $7 \times 7 = \mathbf{49}$.

Backwards: if the **area is 49**, the side is 7 (because $7 \times 7 = 49$), so the perimeter is **28**. If the **perimeter is 36**, the side is $36 \div 4 = 9$, so the area is **81**.

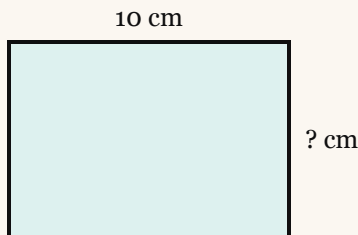


$$\text{side 7: } P = 28, A = 49$$

3 • Perimeter to a missing side

A rectangle has perimeter **34 cm** and length **10 cm**. Two lengths use 20 cm. The rest, $34 - 20 = 14$, is two widths, so the width is **7 cm**.

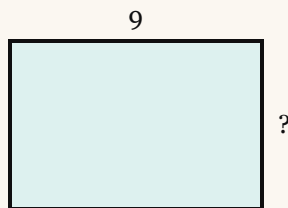
Now the area: $10 \times 7 = \mathbf{70 \text{ square cm}}$. Perimeter $\rightarrow$ missing side $\rightarrow$ area is a favorite test chain.



$P = 34$, length 10, so width 7 and $A = 70$

4 • Area to a missing side

Area **54**, length **9**: $9 \times ? = 54$, so the width is $54 \div 9 = \mathbf{6}$. Perimeter: $2 \times (9 + 6) = \mathbf{30}$.



$A = 54$, length 9, so width 6 and $P = 30$

5 • Area minus perimeter

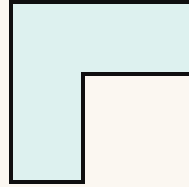
Tests love this: "A rectangle is 12 cm long and 4 cm wide. What is the **difference** between its area and its perimeter?" Area 48, perimeter 32, difference $48 - 32 = \mathbf{16}$.

Work out both numbers first, then subtract. Do not mix the two up.

6 • Odd shapes

Cut an L shape into two rectangles, find each area, and add. For the perimeter, walk every edge: opposite sides across a notch still add up to the full width and height.

An L that fits in a 9 by 9 square has the **same perimeter** as that square (36), but less area.

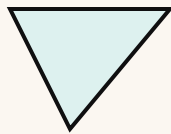


cut into rectangles for area; walk the edges for perimeter

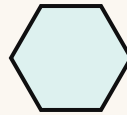
7 • Triangles and other polygons

Perimeter works for any shape: add every side. A triangle with sides 16, 13, and 10 has perimeter **39 cm**.

A regular polygon has equal sides, so multiply: a regular hexagon with side 8 has perimeter $6 \times 8 = 48$.



triangle: add the three sides



regular hexagon: $6 \times \text{side}$

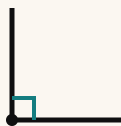
8 • Angles: right, acute, obtuse, straight

A **right angle** is a square corner, 90° . **Acute** is less than 90° . **Obtuse** is more than 90° but less than a straight line. A **straight angle** is 180° , a straight line.

A full turn is 360° . A half turn is 180° . A quarter turn is one right angle, 90° .



acute



right, 90°



obtuse

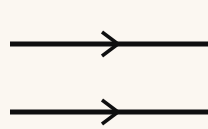


straight, 180°

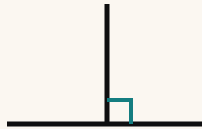
9 • Parallel and perpendicular

Parallel lines run side by side and never meet, like train tracks. **Perpendicular** lines cross at a right angle, like a plus sign.

Lines that cross at any other angle are just intersecting.



parallel



perpendicular

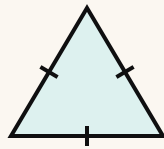


intersecting, not perpendicular

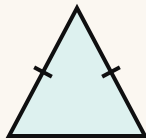
10 • Naming triangles

By sides: **equilateral** (3 equal), **isosceles** (2 equal), **scalene** (none). By angles: **right** (one 90°), **acute** (all under 90°), **obtuse** (one over 90°).

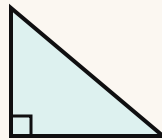
A triangle can have two names: a right isosceles triangle has a square corner and two equal sides.



equilateral



isosceles



right



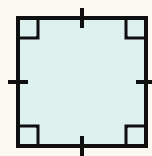
obtuse

11 • Naming quadrilaterals

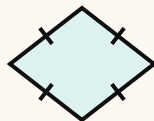
Square: 4 equal sides, 4 right angles. **Rectangle:** 4 right angles. **Rhombus:** 4 equal sides.

Parallelogram: 2 pairs of parallel sides. **Trapezoid:** exactly 1 pair.

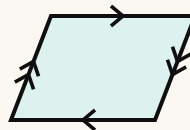
Every square is also a rectangle, a rhombus, and a parallelogram. Rules stack.



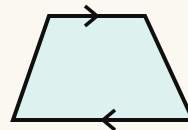
square



rhombus



parallelogram

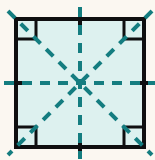


trapezoid

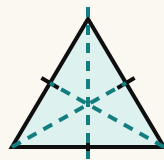
12 • Symmetry

A **line of symmetry** folds a shape onto itself. A square has 4, a rectangle has 2, an equilateral triangle has 3, a circle has endless lines.

A parallelogram that is not a rectangle or rhombus has **none**, even though it looks balanced. You are ready for the test! 🎉



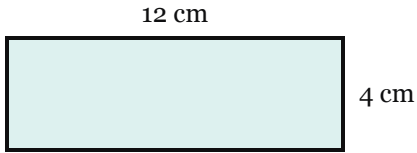
square: 4 lines



equilateral: 3 lines

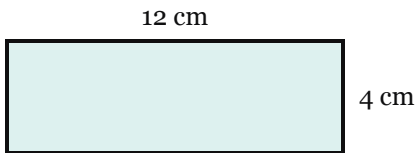
Read each drawing first, then choose the best answer. Take your time, there is no clock here. Questions start gentle and get harder toward the end. Circle your answer.

- 1 A rectangle is 12 cm long and 4 cm wide. What is its perimeter?



- A 48 cm B 32 cm
C 16 cm D 24 cm

- 2 What is the area of the same rectangle?

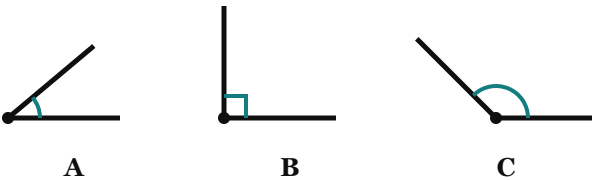


- A 32 square cm B 16 square cm
C 24 square cm D 48 square cm

- 3 A triangle has sides 16 cm, 13 cm, and 10 cm. What is its perimeter?

- A 39 cm B 29 cm
C 26 cm D 49 cm

- 4 Which angle is obtuse?



- A A B B
C C D None of them

5 A square has sides of 7 m. What is its area?

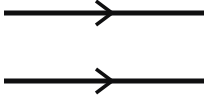
A 28 square m

B 14 square m

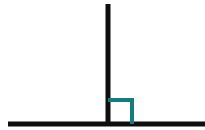
C 21 square m

D 49 square m

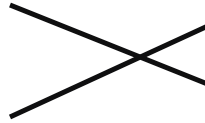
6 Which pair of lines is perpendicular?



A



B



C

A A

B B

C C

D A and C

7 A square has an area of 49 square m. What is its perimeter?

A 49 m

B 14 m

C 28 m

D 196 m

8 How many degrees are in a right angle?

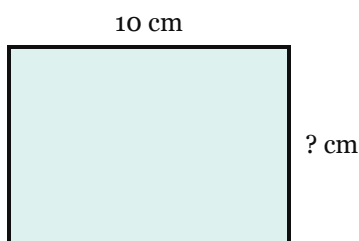
A 90°

B 180°

C 45°

D 360°

9 A rectangle has a perimeter of 34 cm and a length of 10 cm. What is its width?



A 24 cm

B 7 cm

C 12 cm

D 17 cm

10 A rectangle is 12 cm long and 4 cm wide. What is the difference between its area and its perimeter?

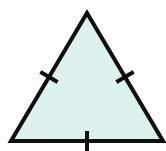
A 48

B 32

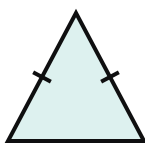
C 8

D 16

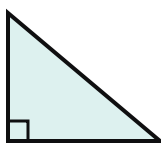
11 Which triangle is isosceles?



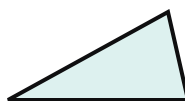
A



B



C



D

A B

B A

C C

D D

12 A square has a perimeter of 36 cm. What is its area?

A 36 square cm

B 9 square cm

C 81 square cm

D 144 square cm

13 Which shape has exactly one pair of parallel sides?

A parallelogram

B rectangle

C rhombus

D trapezoid

14 How many lines of symmetry does a rectangle (that is not a square) have?

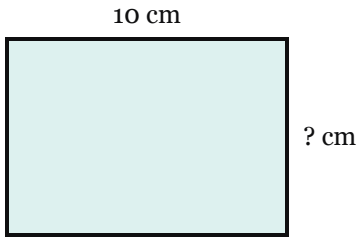
A 4

B 2

C 1

D 0

- 15 A rectangle has a perimeter of 34 cm and a length of 10 cm. What is its area?



- A 340 square cm B 34 square cm
C 70 square cm D 240 square cm
-

- 16 A square has an area of 121 square m. What is its perimeter?

- A 44 m B 121 m
C 22 m D 484 m
-

- 17 A rectangle has an area of 54 square cm and a length of 9 cm. What is its perimeter?

- A 30 cm B 63 cm
C 24 cm D 15 cm
-

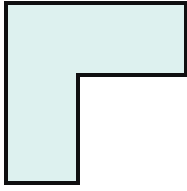
- 18 How many degrees is a half turn?

- A 90° B 360°
C 180° D 45°
-

- 19 A regular hexagon has a perimeter of 48 cm. How long is each side?

- A 6 cm B 12 cm
C 42 cm D 8 cm
-

- 20 This L shape fits inside a 9 by 9 square, with a 6 by 6 corner cut away. What is its area?



- A 81 square units
B 45 square units
C 36 square units
D 54 square units

- 21 Which statement is true?

- A Every rhombus is a square.
B Every rectangle is a square.
C Every square is a rhombus.
D Every trapezoid is a parallelogram.

- 22 Two rectangles have the same perimeter of 20 cm. One is 8 by 2, the other is 6 by 4. How much bigger is the larger area?

- A 8 square cm
B 4 square cm
C 16 square cm
D 24 square cm

- 23 A triangle has one angle of 90° and two equal sides. What is it called?

- A an equilateral triangle
B a right isosceles triangle
C an obtuse scalene triangle
D an acute triangle

- 24 A rectangle is twice as long as it is wide. Its perimeter is 30 cm. What is its area?

- A 30 square cm
B 60 square cm
C 25 square cm
D 50 square cm

ANSWER KEY & EXPLANATIONS

- 1 B** $2 \times (12 + 4) = 32$ cm.
-
- 2 D** $12 \times 4 = 48$ square cm.
-
- 3 A** $16 + 13 + 10 = 39$.
-
- 4 C** C opens wider than a right angle.
-
- 5 D** $7 \times 7 = 49$.
-
- 6 B** B crosses at a right angle.
-
- 7 C** $7 \times 7 = 49$, so each side is 7. $4 \times 7 = 28$.
-
- 8 A** A right angle is a quarter turn, 90° .
-
- 9 B** Two lengths are 20. $34 - 20 = 14$ is two widths, so 7.
-
- 10 D** Area 48, perimeter 32. $48 - 32 = 16$.
-
- 11 A** B has exactly two equal sides (the tick marks).
-
- 12 C** $36 \div 4 = 9$ per side. $9 \times 9 = 81$.
-
- 13 D** The other three have two pairs.
-
- 14 B** One through the middle each way. The diagonals do not work.
-
- 15 C** Width $= (34 - 20) \div 2 = 7$. Area $10 \times 7 = 70$.
-
- 16 A** $11 \times 11 = 121$. $4 \times 11 = 44$.
-
- 17 A** Width $54 \div 9 = 6$. Perimeter $2 \times (9 + 6) = 30$.
-
- 18 C** A full turn is 360° , so half is 180° .
-
- 19 D** Six equal sides: $48 \div 6 = 8$.
-
- 20 B** $9 \times 9 = 81$, minus the $6 \times 6 = 36$ corner: 45.
-
- 21 C** A square has 4 equal sides, so it fits the rhombus rule. The reverse needs right angles.
-
- 22 A** $8 \times 2 = 16$ and $6 \times 4 = 24$. $24 - 16 = 8$.
-
- 23 B** One right angle makes it right; two equal sides make it isosceles.
-
- 24 D** Width w , length $2w$: $2 \times (w + 2w) = 6w = 30$, so $w = 5$ and length 10. Area $5 \times 10 = 50$.
-